

# CS21: Decidability and Tractability

## course information and tentative schedule

**Catalog description:** This course introduces the formal foundations of computer science, the fundamental limits of computation, and the limits of efficient computation. Topics will include automata and Turing machines, decidability and undecidability, reductions between computational problems, and the theory of NP-completeness.

### Course Information:

- Instructor: Chris Umans ([umans@cs.caltech.edu](mailto:umans@cs.caltech.edu))
- TAs:
  - Ricardo Garcia ([ragarcia@caltech.edu](mailto:ragarcia@caltech.edu))
  - Nilo Rivera ([nrivera@caltech.edu](mailto:nrivera@caltech.edu))
  - Ryan Hu ([rrhu@caltech.edu](mailto:rrhu@caltech.edu))
  - Allison Xin ([axin@caltech.edu](mailto:axin@caltech.edu))
  - Emily Parnell ([eparnell@caltech.edu](mailto:eparnell@caltech.edu))
- Lectures: Mondays, Wednesdays, and Fridays 1:00 – 1:55
- Office hours: TBD (1 on Monday night, 2 on Tuesday afternoons, 3 on Tuesday nights)
- Text: *Introduction to the Theory of Computation – 3rd Edition* by M. Sipser (required). Earlier editions should also suffice; the main difference is that they do not have solutions to selected problems.
- Webpage: <http://www.cs.caltech.edu/~umans/cs21/>

**Homework:** The homework is extremely important – for this material, the best way to learn is by doing. I strongly encourage you to work in groups of two or three on the homework. However, you must each turn in your own write-up and note with whom you worked. The rules on homework are:

- There are 7 problem sets. They are released at the end of the Wednesday lecture, and they are due at the beginning of class (1pm) the following Wednesday.
- The quality (clarity, conciseness, neatness) of your write-up counts.
- You may elect to take a two-day extension (until 5pm Friday) on *one* problem set without penalty. Other problem sets turned in late, but before 5pm Friday, receive half credit. You don't need to notify me or the TAs if you are taking the free extension.
- We will be using Gradescope for turning in assignments, and online grading.

**Exams:** There will be a midterm and final exam. They will be indistinguishable from the problem sets, except that they will be cumulative, and you may not work with others on the exams. The homework rules apply to exams as well. There are no extensions for the exams, and no partial credit for exams that are turned in late.

**Honor code:** For homework and exams, you may consult *only* the following material: (1) lecture slides and problem sets posted on the class webpage, (2) solution sets for problem sets you have already turned in, (3) course notes you or others took during lecture, and (4) the required text (Sipser). **I am well aware that there is material from past iterations of this course readily available (online and elsewhere). You may not seek out, study from, or otherwise consult this material during the term, starting now (January 6, 2025).** Please feel free to ask me for clarification if any of these guidelines are unclear.

**Collaboration policy:** Collaboration on problem sets is encouraged, and you may work together in small groups to figure out a solution, including working out details of parts that are challenging or may require a clever trick. You must however turn in your own writeup that may draw on *ideas* from your group, even in detail, but *you may not use or look at the completed work of others*. The writeup should note with whom you

worked. You are individually responsible for learning and understanding the course material in preparation for the exams, and this is not likely to happen if you rely too heavily on your collaborators!

**Reading:** The webpage will list reading in Sipser (3rd edition) that parallels the lectures (when applicable). This is mainly for reference; the lectures are designed to be self-contained.

**Feedback:** If you have any comments or concerns on issues like: the pace of the lectures, the difficulty of the material, time spent on problem sets, or anything else, please let me know! You can tell me or the TAs directly, or you can talk to the course ombudsperson (we will select someone for this role after the first couple of lectures).

**Evaluation and Grades:** Your grade will be based on the following (weighted) components:

Homework 60%; Participation 10%; Midterm 15%; Final 15%.

Each of the 7 problem sets contributes equally to the Homework portion of the grade (i.e., each problem set is worth  $\approx 8.57\%$  of your overall grade).

If you earn 90% of the available (weighted) points you are guaranteed at least an A of some form, 80% guarantees at least a B of some form, 70% guarantees at least a C of some form, etc... *If you are taking the course pass/fail, you need to earn a C- or higher to pass.*

**Tentative lecture schedule:**

#	Date	Subject	Assignments	Reading
1	Jan. 6	Introduction; Finite Automata and Regular Expressions		
2	Jan. 8	Finite Automata and Regular Expressions		
3	Jan. 10	Finite Automata and Regular Expressions		
4	Jan. 13	Pushdown Automata and Context Free Grammars	HW1	
5	Jan. 15	Pushdown Automata and Context Free Grammars		
6	Jan. 17	Pushdown Automata and Context Free Grammars		
-	Jan. 20	NO CLASS: MLK Day (Institute Holiday)	HW2	
7	Jan. 22	Turing Machines, undecidability, and reductions		
8	Jan. 24	Turing Machines, undecidability, and reductions		
9	Jan. 27	Turing Machines, undecidability, and reductions	HW3	
10	Jan. 29	Turing Machines, undecidability, and reductions		
11	Jan. 31	Turing Machines, undecidability, and reductions		
12	Feb. 3	Turing Machines, undecidability, and reductions	Midterm	
13	Feb. 5	Turing Machines, undecidability, and reductions		
14	Feb. 7	Gödel Incompleteness Theorem		
15	Feb. 10	Introduction to Complexity	HW4	
16	Feb. 12	Complexity Classes: P, EXP, and NP		
17	Feb. 14	Complexity Classes: P, EXP, and NP		
-	Feb. 17	NO CLASS: President's Day (Institute Holiday)	HW5	
18	Feb. 19	NP-completeness and reductions		
19	Feb. 21	NP-completeness and reductions		
20	Feb. 24	NP-completeness and reductions	HW6	
21	Feb. 26	[drop day] NP-completeness and reductions		
22	Feb. 28	NP-completeness and reductions		
23	Mar. 3	More complexity classes	HW7	
24	Mar. 5	More complexity classes		
25	Mar. 7	More complexity classes		
26	Mar. 10	Topics: randomized computation	Final	
27	Mar. 12	Topics: quantum computation		
-	Mar. 19		Final due	